Worksheet 0 - Sets Thursday, August 29, 2024 Name:

Two sets are *disjoint* if their intersection is empty. Write your answer either as a finite set, an interval, the union of disjoint intervals, or the union of a finite set and one or more disjoint intervals.

Exercise 1. Consider the following sets of natural numbers.

- $A = \{ n \in \mathbb{N} \mid n \le 25 \}$
- $E = \{ n \in A \mid n \text{ is even} \}$
- $O = \{ n \in A \mid n \text{ is odd} \}$
- $P = \{ n \in A \mid n \text{ is prime} \}$
- $S = \{ n \in A \mid n \text{ is a square} \}$

Compute the following sets.

- (a) P
- **(b)** S
- (c)  $S \cup P$
- (d)  $E \cap S$
- (e)  $(P \cup S) \cap O$
- (f)  $(O \setminus P) \cap (O \setminus S)$
- (g)  $(O \cap S) \times (E \cap S)$

Exercise 2. Consider the following intervals of real numbers.

- A = [0, 10]
- B = (4, 12)
- C = (-5, 7]
- D = [-3, 13)
- E = (5, 15]

Compute the following sets.

- (a)  $A \cup B$
- (b)  $A \cap B$
- (c)  $(A \cup B) \setminus (A \cap B)$
- (d)  $(C \cup D) \setminus B$
- (e)  $(C \cap D) \cup B$
- (f)  $C \setminus D$
- (g)  $A \cup E$
- (h)  $A \cap E$
- $(i)' D \setminus A$

Exercise 3. Compute the following sets of real numbers.

- (a) $A = [1, 20] \cap \mathbb{Z}$
- **(b)**  $B = (5, 10) \cap A$
- (c)  $C = [8, 11] \cap A$
- (d)  $D = (B \cup C) \setminus (B \cap C)$
- (e)  $E = [3, 10] \setminus D$
- (f)  $F = (5, 18) \setminus E$

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Answer 1. Answers to Exercise 1.
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- (a) {2,3,5,7,11,13,17,19,23}
- **(b)** {1, 4, 9, 16, 25}
- (c) {1, 2, 3, 4, 5, 7, 9, 11, 13, 16, 17, 19, 23, 25}
- **(d)** {4, 16}
- (e)  $\{1, 3, 5, 7, 9, 11, 13, 17, 19, 23\}$
- **(f)** {15, 21}
- (g)  $\{(1,4),(1,16),(9,4),(9,16),(25,4),(25,16)\}$

## **Answer 2.** Answers to Exercise 2.

- (a) [0, 12)
- **(b)** (4, 10]
- (c)  $[0,4] \cup (10,12]$
- $(\mathbf{d})$   $(-5, 4] \cup [12, 13)$
- (e) [-3, 12)
- (f) (-5, -3)
- (g) [0, 15]
- (h) (5, 10]
- (i)  $[-3,0) \cup (10,13)$

## **Answer 3.** Answers to Exercise 3.

- (a)  $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20\}$
- **(b)**  $\{6,7,8,9\}$
- (c)  $\{8, 9, 10, 11\}$
- (d)  $\{6, 7, 10, 11\}$
- (e)  $[3,6) \cup (6,7) \cup (7,10)$
- (f)  $\{6,7\} \cup [10,18)$